

Generation and Optimization of Inspection Routes for Economic and Food Safety

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Abstract: Artificial intelligence techniques have been applied to diverse business and governmental areas, in order to take advantage of the huge amount of information that is generated within specific organizations or institutions. Business intelligence can be seen as the process of converting such information into actionable knowledge, which is the basis for data-driven decision making. With this in mind, this work is framed in a project that seeks to improve the activity of the Portuguese Food and Economic Safety Authority, regarding prevention in the areas of food safety and economic enforcement. More specifically, this paper focuses on the generation and optimization of flexible inspection routes. An optimal inspection route seeks to maximize the number of targeted Economic Operators, or the utility gained from the set of Economic Operators that are actually inspected. For that, each Economic Operator is assigned an inspection utility value. The problem was then modelled as a Multi-Depot Periodic Vehicle Routing Problem with Time Windows, and solved using both exact and meta-heuristic methods. The comparison of the meta-heuristic algorithms showed a versatile Hill Climbing implementation in different test cases that explored the effect of the Economic Operators dispersion and density.

1 INTRODUCTION

A considerable amount of work has been developed, throughout the last decades, in the areas of Artificial Intelligence (AI) and machine learning. Such technological advancements have been used successfully as components of decision support systems in private organizations. Governments and public administration institutions have also started to follow this trend and use AI techniques not only to extract useful knowledge from their huge amounts of data, but also to optimize their processes.

The work presented in this paper is part of a broader project, that seeks to improve the activity of the Portuguese Food and Economic Safety Authority (ASAE), regarding prevention in the areas of food safety and economic enforcement. The mentioned

organism is an authority in Portugal, whose mission is to supervise and prevent non-compliance with the national and European legislation regarding the food and non-food sectors. It is also responsible for risk assessment and reporting of hazards detected in the food chain. For that, it is a reference entity in consumer protection, public health, safeguarding market rules and free competition by providing a public service of excellence.

The contribution of this work is related with a complex problem of generation and optimization of inspection routes to surveil Economic Operators. For that, it is necessary to develop models for inspection utility assessment and procedures for selection of relevant Economic Operators in need to be inspected from large amount of registered and geographical sparse number of agents. Moreover, due the mission and area of influence of this entity, it is important to use as much information as possible such as risk matrices and number and type of complaints per Eco-

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nomic Operators. The inspection routes generation process must be capable of maximizing the number of inspections to Economic Operators that present a high inspection utility. The solutions found should be adaptable upon suggestions by the user, reflecting the nature of the work of the human inspectors. Previous research has shown that vehicle routing optimization can promote significant economic savings (Hasle et al., 2007; Toth and Vigo, 2002; Cattaruzza et al., 2017).

The problem was modelled under the Vehicle Routing Problem (VRP) family, as it tries to find the optimal route for a fleet of vehicles that maximizes the global utility of the Economic Operators selected for inspection. Due to specific constraints that need to be taken into account, such as opening hours of Economic Operators, the existence of multiple operational units and the need to extend the planning to multiple days the VRP formulation needs to be expanded.

In Section 2, the related work is discussed. The details about current processes, data size and the routing problem formulation are given in Section 3. Section 4 explains the main choices regarding the implementation of the algorithms to best solve the problems. Several experiments were performed and their details and results appear in Section 5. In Section 6 the paper's conclusions and some suggestions for future work are presented.

2 RELATED WORK

The VRP can be described as a complex combinatorial optimization problem that, given a fleet of vehicles with uniform capacity, a common depot, and several customer demands, find the set of routes with overall minimum route cost which service all the demands (Machado et al., 2002). One of the first problems modeled as a VRP was the *Truck Dispatching Problem* (Dantzig and Ramser, 1959). As stated by the authors, it may be considered as a generalization of the *Traveling Salesman Problem* (TSP) (Flood, 1956; Kruskal, 1956).

A VRP can be modeled as a weighted graph

$$\mathcal{G} = (\mathcal{V}, \mathcal{A}, C)$$

where: $\mathcal{V} = \{v_0, v_1, \dots, v_n\}$ is a set of vertices representing various cities or customers to visit and the depot is indicated by vertex v_0 ; $\mathcal{A}$ is the set of arcs joining these vertices; C is a matrix of non-negative distances c_{ij} associated with each arc (v_i, v_j) , for $i \neq j$. In some cases, the distances may be interpreted as travel costs or travel times. There is also a set of m vehicles

available at the depot. The purpose of the problem is to determine the lowest cost vehicle route set, subject to the following restrictions (Laporte, 1992): (i) each city is visited exactly once by exactly one vehicle; and (ii) all vehicle routes start and end at the depot.

This problem can be mathematically expressed by a set of four equations modeling the objective function and the restrictions (Cardoso, 2009; Toth and Vigo, 2002). Given that, x_{ijk} is a binary decision variable taking the value of 1 if vehicle k traverses the arc (v_i, v_j) , and 0 otherwise and c_{ij} defined as above, the minimum sum of costs of all the arcs is given by Equation 1:

$$\min \sum_{k=1}^m \sum_{i=0}^n \sum_{j=0}^n c_{ij} x_{ijk} \quad (1)$$

Equation 2 limits to one visit per vertex, with exception of the depot:

$$\sum_{i=0}^n \sum_{k=1}^m x_{ijk} = 1, \forall j > 0 \quad (2)$$

Equation 3 ensures that the number of the vehicles arriving at every customer and entering the depot is equal to the number of the vehicles leaving:

$$\sum_{j=0}^n x_{jik} = \sum_{j=0}^n x_{ijk}, \forall i \geq 0, i \neq j, \forall k = 1, \dots, m \quad (3)$$

Equation 4 ensures that all vehicle depart from the depot:

$$\sum_{j=1}^n \sum_{k=1}^m x_{0jk} = |K| \quad (4)$$

This family of problems has been studied intensively over the last few years. In general, they are associated with specific problems of supplying products to customers, supplying supermarket chains or collecting waste from a locality.

Because of the diversity of applications of the VRP problem, several variants have been proposed from adding or removing constraints from the definition (Braekers et al., 2016; Weise et al., 2009). Some of the most well known variations are: the VRP with Time Windows (VRPTW) that is obtained by assigning a time window to each customer (Caric and Gold, 2008; Zhu, 2000); the Multi-Depot VRP (MDVRP) which accommodates more than one depot (Ho et al., 2008; Montoya-Torres et al., 2015); the Periodic VRP (PVRP) that considers multiple days planning (Campbell and Wilson, 2014); the Capacitated VRP (CVRP) where the vehicles have capacity constraints (Breslin and Keane, 1997); or the Open VRP (OVRP) which does not require the vehicle to end the route in the depot (Li et al., 2007).

All the mentioned VRP variants consider routes planning for a single time instant, with exception of the PVRP. The PVRP is a multi-day model where it is possible to choose the day(s) to serve a customer from a set of possible dates. This ability overrules the constraint in Equation 2. The following elements are added to the classical VRP:

- i $\mathcal{T}$ days horizon and
- ii a list of feasible days where the customers can be visited.

For each day defined in $\mathcal{T}$, a VRP is then solved. Evidently, the choice of the visiting schedules and the definition of the routes are interrelated problems (Angelelli and Grazia Speranza, 2002). There exist also a PVRP formulated in Cordeau et al. (1997) that combines the service time (visit duration for each customer) with a work shift for each vehicle (a maximum duration of a route).

Although the study of such methods is not a recent topic, the discussion on how to best solve them is something that still remains today. The reason behind that is that the TSP, the VRP and its variant problems are NP-hard since they are not solved in polynomial time (Caric and Gold, 2008).

There are exact approaches that always determine the optimal solution to the problem, but because they require a high computational power they are only feasible in small data sets. On the other hand, heuristic and meta-heuristic approaches can return solutions close to the optimum and present lower (and often adjustable) execution times, even for large data sets. The difference between these two categories is related to the behaviour of algorithms when determining the solution (Laporte, 1992). To the best of our knowledge, a Tabu Search heuristic is the most explored technique to solve the Periodic Vehicle Routing Problem with Time Windows (PVRPTW) and the Multi-Depot Vehicle Routing Problem with Time Windows (MDVRPTW) separately (Cordeau et al., 2001).

3 INSPECTIONS ROUTE PROBLEM

In this section it is given an overview of the dataset dimension used in this paper followed by the formulation of the problem.

3.1 Dataset Description

The Authority has currently registered more than 3,500,000 Economic Operators in their internal database. More than 200,000 customer complaints

against Economic Operators are registered in an annual basis, both via the complaint book and into ASAE's website. The number of complaints, the infractions implied by them and the type of economic activity will determine the utility of inspection. Consequently, complaint-targeted Economic Operators should be more likely to be included in inspection operations.

The organic structure of the Authority has a nationwide coverage divided into three regional units each divided into variable number of operational units (total of twelve operational units). Each operational unit has a specific number of inspectors and vehicles at their disposal.

The information system in use relies on multiple data sources and platforms. All the referred factors make it very difficult to automate some processes, such as the identification of the Economic Operators that need to be supervised (a time-consuming manual procedure), the assignment of these Economic Operators to brigades of inspectors, or the determination of optimal inspection routes taking into consideration the minimization of travel distances or time.

It is noticeable that there is scope for improvement in the visualization of georeferenced information (Economic Operators) and in the inspections planning. Regarding the inspections planning it is possible to enhance the selection of Economic Operators that maximize the usefulness of being inspected and also the flexible routes generation for the inspectors while minimizing the spent resources.

3.2 Formulation

With respect to the routing problem at hands, it falls into the family of vehicle routing problems as it tries to find the set of inspection routes that maximize the global inspection utility of Economic Operators. Given the specific inherent constraints of inspection routing, it is possible to classify the problem as a Multi-Depot Periodic Vehicle Routing Problem with Time Windows (MDPVRPTW) (Cordeau et al., 2002). An example of a geographical representation of a solution of MDPVRPTW with four routes starting (and ending) from three operational units (orange circles) and visiting thirteen Economic Operators (blue circles) are shown in Figure 1.

The main differences between this modelling of the problem as a MDPVRPTW and the classical VRP are:

- i the Multi-Depot takes into account the existence of more than one depot where the vehicles starts and arrives;

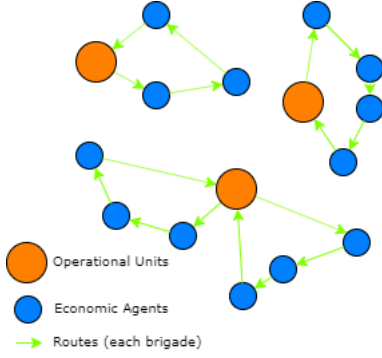


Figure 1: MDPVRPTW representation.

- ii the Periodic nature establishes a multi-day planning with the ability to choose when to visit an Economic Operator; and
- iii the Time Windows set a list of visiting schedules when each Economic Operator can be visited.

This family of route generation problems encompasses the main constraints of the route inspection problem within the geographical limits of an operational unit follows the flow-based formulation below.

The problem can be also modeled as a graph

$$\mathcal{G}(\mathcal{V}, \mathcal{A}, c)$$

where $\mathcal{V} = \mathcal{EO} \cup \mathcal{D}$ is a set of nodes composed of depots $\mathcal{D} = \{v_1, \dots, v_{|\mathcal{D}|}\}$ and Economic Operators $\mathcal{EO} = \{v_{|\mathcal{D}|+1}, \dots, v_{|\mathcal{D}|+|\mathcal{EO}|}\}$. The set of arcs that connect these nodes is $\mathcal{A} = \{(i, j) : i, j \in \{1, \dots, |\mathcal{V}|\}, i \neq j, \{i, j\} \not\subset \mathcal{D}\}$. There is also a set of brigades $\mathcal{B}$ which will perform the inspections. Each brigade $b \in \mathcal{B}$ is a combination of a vehicle w (from a set $\mathcal{W}$ of all available vehicles) and a set of inspectors I_b (from a set I of all inspectors) where $|I_b| \geq 2, \forall b \in \mathcal{B}$. Similar to Cordeau et al. (1997), each brigade $b \in \mathcal{B}$ has also an associated work shift $[SS_b, ES_b]$, where SS and ES are starting and ending of the work shift time, respectively. Each Economic Operator $eo \in \mathcal{EO}$ has a set of associated time windows OH_{EO} which correspond to the opening hours where they can be inspected. $OH_{EO} = \{[ot_j, ct_j]_{eo} : j = 1, \dots\}$ where ot_j and ct_j are the opening and closing times of consecutive working periods j in a day, respectively. Thus, a brigade has to wait if the time of arrival at Economic Operator eo is not between any pair of $[ot_j, ct_j] \in OH_{eo}$. Each brigade $b \in \mathcal{B}$ has a foreseen break time $BT = [bs_b, be_b]$ of fixed size. Every $eo \in \mathcal{EO}$ has an expected time of inspection ti_{eo} according to the type of their economic activity, e_{eo} . Another key factor is the $u_{eo} \in [0, 1]$ which corresponds to the utility of inspecting Economic Operator eo .

The objectives for this paper are either the maximization of the global utility (defined in Equation 5)

or the maximization of the number of inspected Economic Operators in each day of inspection planning (defined in Equation 6). They must be achieved while satisfying the constraints for the classical VRP with Multi-Depot, the time window of each Economic Operator and the brigade's work shift.

$$\max \sum_{b \in \mathcal{B}} \sum_{i \in \mathcal{V}} \sum_{j \in \mathcal{EO}} u_j x_{ijb} \quad (5)$$

$$\max \sum_{b \in \mathcal{B}} \sum_{i \in \mathcal{V}} \sum_{j \in \mathcal{EO}} x_{ijb} \quad (6)$$

This formulation makes the present problem of route generation a very challenging one from a technical point of view. The solution here presented required some relaxation of constraints in order to obtain results in a reasonable amount of time.

4 FLEXIBLE ROUTES GENERATION

The methodologies implemented to solve the problem involved one exact method and three meta-heuristic methods. In Section 4.1 the notion of inspection utility is detailed, and in Section 4.2 the representation of the solution is presented. Then, the details of the implemented algorithms are included in Sections 4.3 and 4.4. Section 4.5 gives an overview of the developed web application to interact with such methods.

4.1 Inspection Utility

The utility u_{eo} of inspecting an Economic Operator is the basis for determining optimal inspection routes, since it is the element that is intended to be maximized when seeking to obtain an optimal inspection route. In the current approach, this value is obtained empirically through the evaluation of customer complaints. Based on this information, we define a utility transformation function, shown in Equation 7. The value of u_{eo} is based on the number of complaints NC regarding Economic Operator eo registered in the system.

$$u_{eo}(NC) = \begin{cases} 0.05 & \text{if } NC = 0 \\ \frac{NC}{10} & \text{if } 1 \leq NC < 10 \\ 0.9 + \frac{NC-9}{100} & \text{if } 10 \leq NC < 19 \\ 1 & \text{if } NC \geq 19 \end{cases} \quad (7)$$

Every Economic Operator has a non-null utility because, even in the absence of complaints, it can be subject to inspection. Economic Operators with $1 \leq NC < 10$ have a transformation with a slope higher

than agents with $10 \leq NC < 19$. Economic Operators with $NC \geq 19$ are classified with the fixed maximum value of $u_{eo} = 1$.

The determination of this function was based on the analysis of the distribution of the number of complaints per Economic Operator, graphically visible in Figure 2 (the vertical axis is in logarithmic scale). The number of agents with $NC < 19$ represent 99.84% of the population of Economic Operators with reported complaints; therefore, above that number of complaints the utility gets its highest value of 1. The decline is more pronounced in Economic Operators that have $1 \leq NC < 10$ since this group represents 99.51% of the population of agents with complaints.

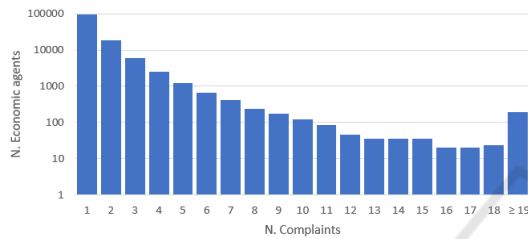


Figure 2: Number of complaints distribution from 2013-2018 (logarithmic Y axis).

4.2 Representation

To obtain the optimal inspection routes for $|\mathcal{B}|$ brigades, routes are represented by a set of $|\mathcal{B}| + 1$ lists. This form of representation allows us to deal with the periodic nature of the VRP, which does not require all Economic Operators to be visited in one day. As the planning is calculated daily, the first $|\mathcal{B}|$ lists include the actual inspection routes, while the last list contains those Economic Operators that are not part of the solution but may be integrated in the next day plan. The generated routes include, for each brigade, the Economic Operators stored by inspection order. As an example, Table 1 represents a solution for 2 brigades and 8 Economic Operators.

Table 1: Solution representation.

Representation		
[6,3,4], [1,8], [2,5,7]		
Brigade 1	Brigade 2	Unused eo
6 → 3 → 4	1 → 8	2, 5, 7

This solution representation is used by all algorithms with exception for the genetic algorithm, which requires another form of representation in order to enable crossover and mutation operations between individuals. This adaptation is achieved by converting the multidimensional list into a linearized single-dimensional one. For the same example illustrated in

Table 1, the representation of the individual in the genetic algorithm is [6, 3, 4, 1, 8, 2, 5, 7]. To decode the individual into the routes solution, each eo is inserted sequentially in the brigades until no more eo fit their work shift duration (Zhu, 2000).

4.3 Exact Approach

The Branch and Bound algorithm is part of the set of exact methods that solve the Vehicle Routing Problem. It always ensures the discovery of the best existing solution, despite its high temporal complexity. For the problem in hands the branching strategy allows to traverse all the solution space by adding each possible Economic Operator to each brigade at a time. The bounding occurs when the generated solution disrespects the work shift duration of any brigade.

The application of the method to the specific problem is shown in Figure 3. The example includes three Economic Operators (1, 2 and 3) with utilities of 0.05, 0.40 and 0.10 respectively. In the first node all the agents compose the set of agents not inspected by any brigade, so the utility of the solution is 0. At each layer, an agent is removed from the last array and inserted into one of the brigades.

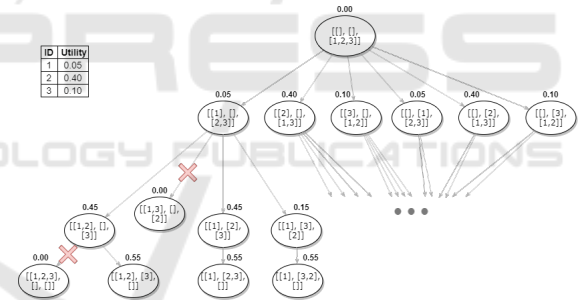


Figure 3: Branch Bound applied to the routing problem.

Although this type of approaches is only practicable with small sized problems, the implementation is useful to perform comparable tests with the other algorithms.

4.4 Meta-heuristic Approaches

Regarding meta-heuristic approaches, three different methods were developed: (i) Hill Climbing, (ii) Simulated Annealing and (iii) Genetic Algorithm. The main details are described in this section.

Hill Climbing and Simulated Annealing allowed to obtain a sufficiently good solution in a short execution time, when compared to the Branch and Bound algorithm, for instance.

In this concrete implementation, the algorithms start by generating an initial valid solution, generated

by trying to allocate Economic Operators in a random way to each brigade, having as limit the work shift of each one. The remaining Economic Operators are kept on the last list. From this solution they proceed to find the optimal solution out of all possible solutions (the search space). The neighborhood function is based on two equiprobable operators (Figure 4):

- *Repositioning* consists of exchanging the position of an Economic Operator, either within the same brigade or to a different brigade (when repositioning an Economic Operator in the last fictitious brigade list, it becomes part of the agents not included in the solution).
- *Swap* consists of changing the order of two Economic Operators; just as with repositioning, swapping can also occur between two agents of the same brigade or different brigades.

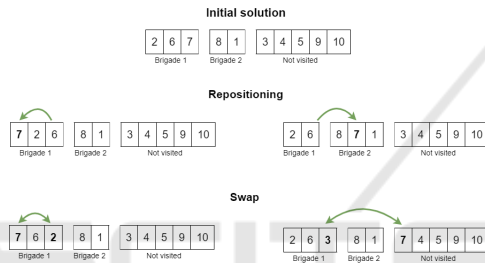


Figure 4: Neighborhood generation operations.

The implementation of Simulated Annealing has the specificity of probabilistically accepting solutions with lower utility than the best solution at the moment. Equation 8 shows the temperature update function, while Equation 9 shows the acceptance probability formula in this specific application of the method.

$$temperature = 1 - \left(\frac{\text{iteration}}{n \text{ of steps}} \right)^{\frac{1}{2}} \quad (8)$$

$$p = e^{\frac{\frac{1}{2} \times \frac{\text{new utility} - \text{utility}}{\text{utility}}}{\text{temperature}}} \quad (9)$$

The probability of accepting solutions with lower utility is related with the differences in utility and the number of iterations already performed. Regarding the implementation of the Genetic Algorithm, the selection process suggested by Zhu (2000) was used – selection by tournament. The implication in this selection scheme is that genetically superior chromosomes are given priority in mating but average entities have some chances of being selected too, provided they happen to be compared with a 'worse-off' chromosome.

Regarding the crossover process, two options were implemented: PMX and heuristic crossover.

The application of common crossover operations unavoidably produces invalid offspring that have duplicated genes in one string. With PMX, two arbitrary points are selected, the portions of the chromosomes between these points are swapped and in order to remove duplicate Economic Operators, a series of gene swappings are performed. This crossover operation originates two descending chromosomes.

Heuristic crossover is a slightly different process because it takes into account the distance between the Economic Operators. It starts with an arbitrary cut on both chromosomes and one of the genes immediately following the cut position is chosen to be maintained. The not selected gene is replaced or deleted to avoid duplication in the following iterations. After this decision, an iterative process begins that traverses the chromosomes and compares, in each iteration i , the distance between the gene at position i and position $i + 1$ of both progenitor chromosomes. The $i + 1$ position gene presenting lower distance is selected to be part of the descending chromosome. The gene that was not selected is either deleted or swapped with the selected gene. In the current implementation, two descendants are generated, one from repositioning and the other from deletion (Zhu, 2000).

After crossover, there is a low probability of mutation in the descending chromosomes. The current implementation encompasses four types of mutations, equally likely to occur:

- *Gene Repositioning*: a gene / Economic Operator is randomly selected and repositioned at a random position inside the chromosome.
- *Sequence Repositioning*: it is similar to the previous operation, however repositioning is performed on a set of consecutive genes.
- *Gene Swap*: two genes / Economic Operators are selected randomly and their positions are swapped.
- *Sequence Swap*: it is similar to the previous operation, however position swapping is performed between a set of consecutive genes and a gene.

4.5 Applicability

A crucial factor for being successful in solving sophisticated vehicle routing problems (VRP) is to offer reliable and flexible solutions (Ritzinger et al., 2016). Taking this into account, an Web application was designed to interact with the logic layer (that solves the problem following the approaches above) and to visualize the solutions from a geographical and chronological point of view.

The Web application shown in Figure 5 is the part of the solution implemented for visualization and interaction with the core of the developed work, where the *Inspections Planning Assistant* is the most relevant for this paper. It contains two main pages: an application page where it is possible to request the generation of inspection routes, consult the solution produced in three different views, change the routes by adding agents to the solution or removing them, and storing the routes permanently. The other page is used to query inspection actions already stored.

The developed system is capable of creating a daily plan for one or more brigades of inspectors in order to promote a maximum number of inspections in a day or to maximize the value of the utility of inspected agents with an efficient use of resources. This way it can work as a decision support system for inspectors. The inspection plan can be consulted by any worker and the system is amenable to evaluation by workers who suggest changes in the route or additions/removals of Economic Operators. These changes affect directly the defined utility of each Economic Operator from the previous solution and therefore the solution is recalculated and presented.

5 RESULTS

Followed by the development of the four algorithms, multiple tests and experiments, in simulated environment, were performed in order to promote a better evaluation of the implemented methods. Based on such experiments, relevant information has been collected regarding algorithms performance, and solutions quality.

Regarding the exact algorithm (Branch and Bound), the capabilities of returning the optimal solution were tested given an execution time limit of 300 seconds. The results are presented in Table 2, which covers executions from 1 to 8 brigades for the maximization of the number of inspected Economic Operators. For 1 brigade it presented a maximum input size of 24 Economic Operators, and 14 Economic Operators for 8 brigades. In the rightmost columns it is possible to verify the execution times for inputs of 4, 8, 12, and 14 Economic Operators.

The evaluation of the meta-heuristic methods varies essentially according to the size and the type of the input data (Economic Operators). The following issues were taken into account:

- The values shown for meta-heuristic methods are always the average of 3 executions.
- Brigades always start their route at the same hour

and their work shift has the same duration. Starting and ending points are also the same.

- For the Genetic Algorithm, executions were performed using a population of 100 individuals, with crossover, mutation and recovery probabilities of 80%, 5% and 4% respectively.

Varying parameters were:

- *Objective Function*: Maximization of the total utility of inspected agents, or maximization of the number of Economic Operators to be inspected.
- *Number of Brigades*: 2 brigades per 100 Economic Operators, or 8 brigades per 100 Economic Operators.
- *Number of Iterations*: 10,000 or 100,000 for Hill Climbing and Simulated Annealing, and 100 or 200 to the Genetic Algorithm.

Varying the objective function and the number of brigades allowed us to analyze the direct effect of these variables in the performance of the final solution.

The test set is shown in Table 3, representing 8 Portuguese municipalities, the number of Economic Operators located in those municipalities, and the travel cost (distance and time) between the municipality and the center of operational unit (Figure 6). The set of municipalities was carefully split into three test subsets. (i) The red subset has only one municipality and a low density of Economic Operators; (ii) the blue subset is composed of four geographically dispersed municipalities, also with low densities; on the other hand, (iii) the orange subset has three municipalities close to the starting/finishing place and a total of 424 Economic Operators.

The results for the referred three subsets are presented in Tables 4, 5 and 6. For each test case we show the number of brigades used to determine the solution, the number of iterations used as stop conditions and the results for the two objective functions: maximization of the global inspection utility ($max u_{eo}$) and maximization of the number of inspected Economic Operators ($max inspected eo$). The $avg u_{eo}$ and the $avg eo$ columns contain the average of obtained inspection utilities and number of inspected Economic Operators, respectively. Regarding the average for the total execution times and the times to determine the best solution, they are displayed in the $avg T$ and the $avg t$ columns, respectively. Through the global analysis of the obtained results it is possible to conclude that they are satisfactory as all the tests returned a possible solution within the previously defined parameters.

Table 4, specifically, allows to compare the three implemented meta-heuristic methods with the exact

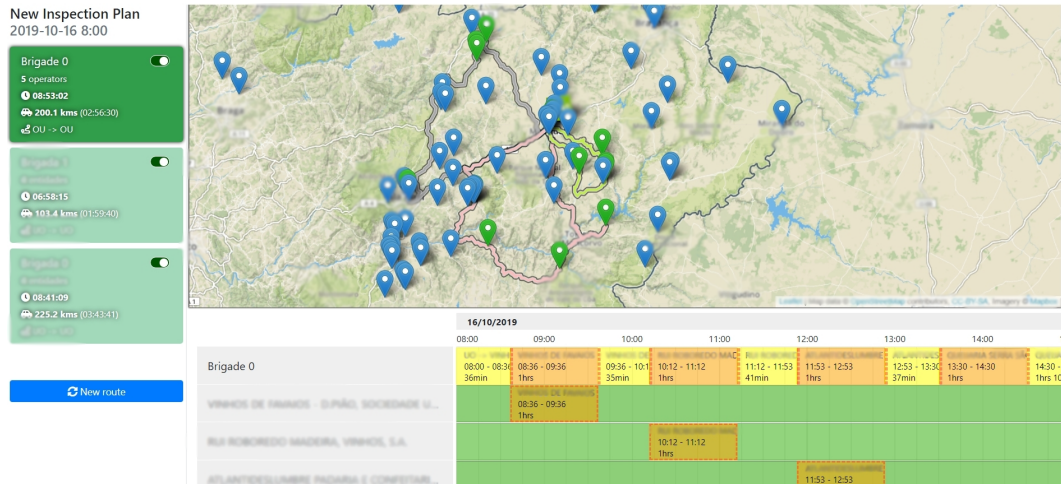


Figure 5: Web application overview.

Table 2: Branch and Bound results.

# Brigades	Max. input <i>eo</i>	Inspected <i>eo</i>	Execution time (secs)			
			4 <i>eo</i>	8 <i>eo</i>	12 <i>eo</i>	14 <i>eo</i>
1	24	7	0.0004943	0.003002	0.083515	0.097988
2	17	9	0.001474	0.012493	0.621539	0.722548
3	16	8	0.003000	0.035997	2.502038	2.944052
4	15	7	0.006986	0.085037	7.63200	8.982038
5	15	6	0.011999	0.167528	19.607051	23.136030
6	14	6	0.021499	0.308495	44.219024	52.153544
7	14	6	0.031999	0.537499	91.563532	107.494027
8	14	6	0.048499	0.871530	175.266998	205.784034

Table 3: Supporting information about each place from test set.

ID	# <i>eo</i>	Dist (km)	Time (mins)
1	32	8.6	14
2	15	9.9	16
3	25	8.2	16
4	32	9.2	12
5	35	10.5	18
6	126	2.3	6
7	150	2.0	6
8	148	2.8	7

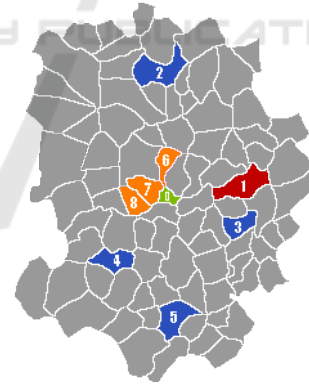


Figure 6: Geographical distribution of the places used in the experiments.

one. For one brigade and the maximization of inspected *eo* it is possible to verify that every algorithm got 7 Economic Operators, the same value as the Branch and Bound, Table 2. The fastest implementation to retrieve this solution is the Hill Climbing, with the lowest *avg t*, followed by the Genetic Algorithm.

Hill Climbing was the most versatile method and capable of returning a solution with high utility in a shorter time period than other meta-heuristic methods. Regardless of the number of Economic Operators, brigades or distribution relative to the operational unit, this was the best performing method.

In theory, Simulated Annealing should allow to

achieve solutions of superior utility than Hill Climbing. However, this has rarely been observed. The main explanation for this phenomenon is due to the equation definition for determining the temperature and probability of acceptance of solutions with inferior utility. Even with equation tuning, Hill Climbing outperformed Simulated Annealing in terms of execution time and solution utility.

As expected, the increment of iterations allowed

Table 4: Case 1 results.

Algorithm	# Brigades	Iterations	max u_{eo}			max inspected eo		
			avg u_{eo}	avg t	avg T	avg eo	avg t	avg T
HC	1	10000	0.035	0.047	0.540	7	0.020	0.574
		100000	0.035	0.038	5.398	7	0.022	5.428
SA	1	10000	0.035	0.156	0.555	7	0.077	0.541
		100000	0.035	0.176	5.368	7	0.354	5.383
GA (PMX)	1	100	0.035	0.033	1.593	7	0.030	1.459
		200	0.035	0.031	2.851	7	0.029	2.868
GA (Heuristic)	1	100	0.035	0.027	2.020	7	0.029	1.989
		200	0.035	0.029	4.385	7	0.038	4.447
HC	3	10000	0.097	0.339	0.724	19	0.211	0.733
		100000	0.100	3.579	7.170	20	2.063	7.276
SA	3	10000	0.092	0.618	0.690	19	0.631	0.710
		100000	0.095	6.283	7.048	19	6.704	7.093
GA (PMX)	3	100	0.095	0.656	2.332	19	0.288	2.164
		200	0.097	0.454	4.631	19	1.300	4.243
GA (Heuristic)	3	100	0.098	1.001	2.893	19	0.423	2.622
		200	0.100	2.748	5.455	20	1.712	5.390

Table 5: Case 2 results.

Algorithm	# Brigades	Iterations	max u_{eo}			max inspected eo		
			avg u_{eo}	avg t	avg T	avg eo	avg t	avg T
HC	3	10000	0.100	0.462	1.328	20	0.812	1.332
		100000	0.105	2.405	12.807	21	1.767	12.747
SA	3	10000	0.093	1.049	1.276	19	1.750	2.013
		100000	0.100	11.400	12.690	20	11.317	12.651
GA (PMX)	3	100	0.095	0.590	3.894	20	1.770	3.933
		200	0.098	2.008	7.790	20	3.254	7.804
GA (Heuristic)	3	100	0.103	2.352	6.664	21	2.857	6.542
		200	0.103	3.994	13.171	21	4.929	13.145
HC	9	10000	0.268	1.355	1.806	54	1.114	1.796
		100000	0.287	9.377	18.000	58	14.304	17.843
SA	9	10000	0.187	1.611	1.638	41	1.628	1.630
		100000	0.263	17.403	17.678	53	16.845	16.934
GA (PMX)	9	100	0.262	4.375	5.887	50	2.824	5.815
		200	0.268	9.897	11.984	53	7.219	12.258
GA (Heuristic)	9	100	0.248	4.514	8.280	47	4.810	8.085
		200	0.250	6.539	16.329	52	12.161	16.534

Table 6: Case 3 results.

Algorithm	# Brigades	Iterations	max u_{eo}			max inspected eo		
			avg u_{eo}	avg t	avg T	avg eo	avg t	avg T
HC	9	10000	1.017	2.692	3.638	63	1.648	3.440
		100000	1.270	11.184	34.606	63	1.869	34.499
SA	9	10000	0.910	3.260	3.297	51	3.255	3.288
		100000	1.085	29.929	34.233	63	33.311	33.582
GA (PMX)	9	100	1.240	9.184	14.733	60	7.205	14.143
		200	1.242	20.861	26.842	63	16.717	28.364
GA (Heuristic)	9	100	0.953	31.613	40.209	57	22.291	40.170
		200	1.055	74.048	80.185	58	56.362	78.068
HC	34	10000	1.218	4.353	4.473	113	4.405	4.542
		100000	2.080	52.686	53.695	228	53.100	54.150
SA	34	10000	0.957	4.082	4.113	66	4.093	4.205
		100000	1.473	46.820	46.878	124	45.202	45.334
GA (PMX)	34	100	1.953	21.786	22.326	201	21.420	22.797
		200	1.992	45.537	46.535	210	36.678	46.717
GA (Heuristic)	34	100	1.752	45.362	48.584	171	36.859	47.450
		200	1.760	79.721	92.696	175	53.993	95.598

to achieve solutions with equal or greater utility in every test case but the added time of execution is considerable.

The analysis of the Genetic algorithm concluded that the heuristic crossover was the best option in the first case studied, where the number of Economic Operators and its dispersion were short. It presented the best solution for 3 brigades alongside Hill Climbing, but with a shorter *avg t*. In the remaining two cases, with higher dispersion and density of Economic Operators, the PMX crossover was the one that allowed to determine solutions with better utility and in a shorter period of time. In general, the addition of brigades under each test case have a greater impact on the execution times for the Genetic algorithm than for the Hill Climbing or the Simulated Annealing.

6 CONCLUSIONS AND FUTURE WORK

In this paper, we presented the modeling and resolution of a complex combinatorial optimization problem related with the inspections planning process of the Portuguese Economic and Food Safety Authority. The definition of the constraints of the problem was important to classify the problem at hands as a MD-PVRPTW. Another key factor was the determination of a utility function capable of determining the inspection utility of an Economic Operator based on the number of associated complaints. Finally, four strategies to solve the routing problem were implemented: one exact and three meta-heuristic approaches. This work is integrated in a Web application targeted to support the decision of the Authority's personnel and enhance current processes of Economic Operators selection for inspection and inspections routing.

The development prospects for a project of this nature and scope are varied. In particular, the flexible inspection route generation module developed includes several perspectives for future development, both in terms of optimization and in terms of additional features:

- Expansion of the number of implemented methods and/or parameters in order to obtain better solutions.
- Inclusion of break-time periods for inspectors and supervisors during the inspection route. The fact that this period is flexible and can be different according to the start time of the inspection actions makes it difficult to add to the methods currently implemented, but should be taken into account in a next version of the system since it compromises

the use of the routes in a real context.

- Addition of different starting and finishing points. Changing the methods for the fulfillment of these conditions is a lengthy process, so the current version only includes solutions to start and end at the same geographic point – the headquarters of the operational unit.
- Test the whole system in the field with the collaboration of the Authority, to extract metrics from algorithms in a real context and detect gaps that are not visible in a simulated environment without professionals in the area.

Within the scope of the project as a whole, there are development prospects that will directly and indirectly affect the module of the generation of flexible routes, such as:

- Implementation of risk matrices that will allow a determination of more accurate inspection utilities. Optionally, the calculation should be changed as new information is extracted from the internal system.
- Development of an inspection durations adaptive approach, based on actual practice. The categorization of average inspection durations per area of activity of Economic Operators will increase the quality of the solutions obtained.

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