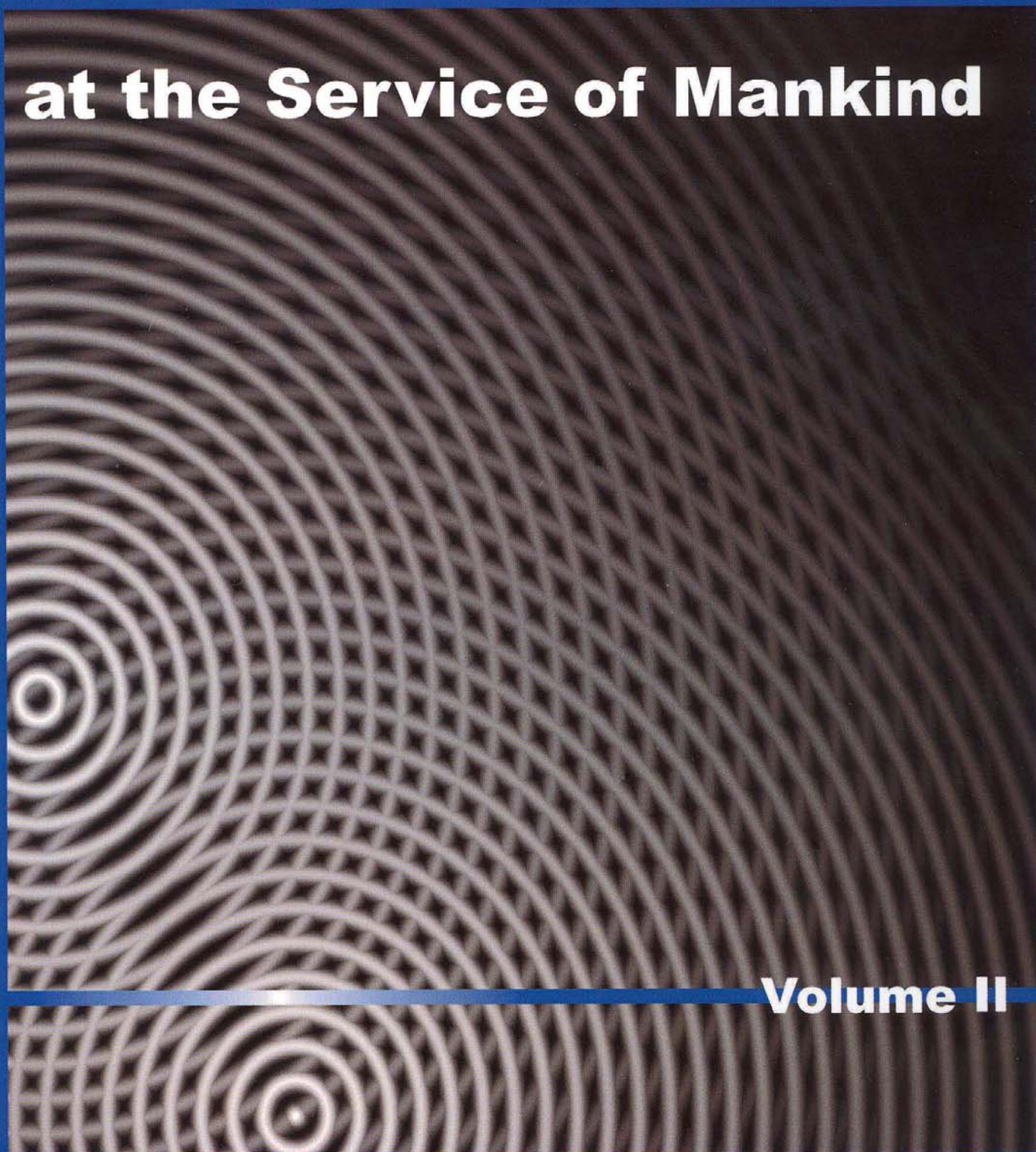


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Gait Selection for Quadruped Legged Robots

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Abstract — *This paper studies periodic gaits of quadruped locomotion systems. The purpose is to determine the best set of gait and locomotion variables for different robot velocities based on the system dynamics during walking. In this perspective, several performance measures are formulated and a set of experiments reveals the influence of the gait and locomotion variables upon those proposed indices. The results show that the locomotion parameters (β , L_S and H_B) should be adapted to the walking velocity in order to optimize the robot performance. Furthermore, for the case of a quadruped robot, we concluded that the gait should be adapted to V_F .*

1 Introduction

Walking machines allow locomotion in terrain inaccessible to other type of vehicles, since they do not need a continuous support surface. However, the requirements for leg coordination and control impose difficulties beyond those encountered in wheeled robots [1]. Gait analysis and selection is a research area requiring an appreciable modelling effort for the improvement of mobility with legs in unstructured environments. Several quadruped robots have been developed which adopt different quadruped gaits such as the bound [2, 3, 4], trot [5] and gallop [6]. Nevertheless, detailed studies on the best set of gait and locomotion variables for different robot velocities are missing. In this line of thought, a simulation model for multi-legged locomotion systems was developed, for several periodic gaits [1, 7]. This study intends to generalize previous work [8, 9, 10] through the formulation of several indices measuring the system dynamics and the hip trajectory errors during forward straight line walking at different velocities.

Bearing these facts in mind, the paper is organized as follows. Section two introduces the robot kinematic model and the motion planning scheme. Sections three and four present the robot dynamic model and control architecture and the optimizing indices, respectively. Section five develops a set of experiments that reveal the influence of the locomotion parameters and robot gaits on the performance measures, as a function of robot body velocity. Finally, section six outlines the main conclusions.

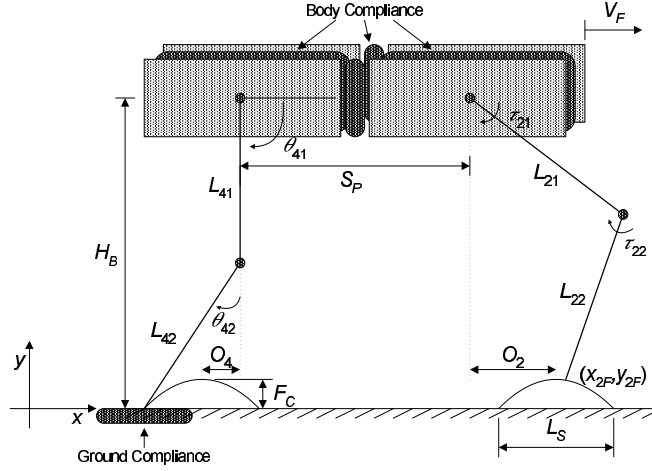


Figure 1: Kinematic and dynamic quadruped robot model

2 Kinematics and Trajectory Planning

We consider a quadruped walking system (Figure 1) with $n = 4$ legs, equally distributed along both sides of the robot body, having each two rotational joints (*i.e.*, $j = \{1, 2\} \equiv \{\text{hip, knee}\}$). Motion is described by means of a world coordinate system. The kinematic model comprises: the cycle time T , the duty factor β , the transference time $t_T = (1 - \beta)T$, the support time $t_S = \beta T$, the step length L_S , the stroke pitch S_P , the body height H_B , the maximum foot clearance F_C , the i^{th} leg lengths L_{i1} and L_{i2} and the foot trajectory offset O_i ($i = 1, \dots, n$).

Gaits describe sequences of leg movements, alternating between transfer and support phases. Given a particular gait and duty factor β , it is possible to calculate, for leg i , the corresponding phase ϕ_i , the time instant where each leg leaves and returns to contact with the ground and the cartesian trajectories of the tip of the feet (that must be completed during t_T) [1].

The robot body, and by consequence the legs hips, is assumed to have a desired horizontal movement with a constant forward speed $V_F = L_S / T$. Concerning the robot feet, we consider a periodic trajectory for each foot, being the trajectory of the swing leg foot, for each cycle, computed through a cycloid function [11]. Based on this data, the trajectory generator produces a motion that synchronizes and coordinates the legs.

The forward motion planning algorithm accepts the desired cartesian trajectories of the legs hips $\mathbf{p}_{Hd}(t) = [x_{iHd}(t), y_{iHd}(t)]^T$ and feet $\mathbf{p}_{Fd}(t) = [x_{iFd}(t), y_{iFd}(t)]^T$ as inputs and, by means of an inverse kinematics algorithm, generates the related joint trajectories $\Theta_d(t) = [\theta_{i1d}(t), \theta_{i2d}(t)]^T$, selecting the solution corresponding to a forward knee [11].

3 Dynamics and Control Architecture

3.1 Inverse Dynamics Computation

The planned joint trajectories constitute the reference for the robot control system. The robot inverse dynamic model is formulated as:

$$\mathbf{\Gamma} = \mathbf{H}(\boldsymbol{\Theta}) \ddot{\boldsymbol{\Theta}} + \mathbf{c}(\boldsymbol{\Theta}, \dot{\boldsymbol{\Theta}}) + \mathbf{g}(\boldsymbol{\Theta}) - \mathbf{F}_{\mathbf{RH}} - \mathbf{J}^{\mathbf{T}}(\boldsymbol{\Theta}) \mathbf{F}_{\mathbf{RF}} \quad (1)$$

where $\mathbf{\Gamma} = [f_{ix}, f_{iy}, \tau_{i1}, \tau_{i2}]^{\mathbf{T}}$ ($i = 1, \dots, n$) is the vector of forces / torques, $\boldsymbol{\Theta} = [x_{iH}, y_{iH}, \theta_{i1}, \theta_{i2}]^{\mathbf{T}}$ is the vector of position coordinates, $\mathbf{H}(\boldsymbol{\Theta})$ is the inertia matrix and $\mathbf{c}(\boldsymbol{\Theta}, \dot{\boldsymbol{\Theta}})$ and $\mathbf{g}(\boldsymbol{\Theta})$ are the vectors of centrifugal / Coriolis and gravitational forces / torques, respectively. The $(m+2) \times 2$ ($m = 2$) matrix $\mathbf{J}^{\mathbf{T}}(\boldsymbol{\Theta})$ is the transpose of the robot Jacobian matrix, $\mathbf{F}_{\mathbf{RH}}$ is the $(m+2) \times 1$ vector of the body inter-segment forces and $\mathbf{F}_{\mathbf{RF}}$ is the 2×1 vector of the reaction forces that the ground exerts on the robot feet. These forces are null during the foot transfer phase.

Furthermore, we consider that the joint actuators are not ideal, exhibiting a saturation given by:

$$\tau_{ijm} = \begin{cases} \tau_{ijC} & , \quad |\tau_{ijm}| \leq \tau_{ijMax} \\ \text{sgn}(\tau_{ijC}) \tau_{ijMax} & , \quad |\tau_{ijm}| > \tau_{ijMax} \end{cases} \quad (2)$$

where, for leg i and joint j , τ_{ijC} is the controller demanded torque, τ_{ijMax} is the maximum torque that the actuator can supply and τ_{ijm} is the motor effective torque.

3.2 Robot Body Model

Figure 1 presents the dynamic model for the quadruped body and foot-ground interaction. It is considered a compliant robot body because most walking animals have a spine that allows supporting the locomotion with improved stability.

In the present study, the robot body is divided in n identical segments (each with mass $M_b n^{-1}$) and a linear spring-damper system is adopted to implement the intra-body compliance according to:

$$f_{i\eta H} = \sum_{i'=1}^u [-K_{\eta H} (\eta_{iH} - \eta_{i'H}) - B_{\eta H} (\dot{\eta}_{iH} - \dot{\eta}_{i'H})] \quad (3)$$

where $(x_{i'H}, y_{i'H})$ are the hip coordinates and u is the total number of segments adjacent to leg i , respectively. In this study, the parameters $K_{\eta H}$ and $B_{\eta H}$ ($\eta = \{x, y\}$) in the {horizontal, vertical} directions, respectively, are defined so that the body behaviour is similar to the one expected to occur on an animal (Table 1).

3.3 Foot-Ground Interaction Model

The contact of the i^{th} robot foot with the ground is modelled through a non-linear system [11] with linear stiffness $K_{\eta F}$ and non-linear damping $B_{\eta F}$ ($\eta = \{x, y\}$) in the {horizontal, vertical} directions, respectively (see Figure 1), yielding:

$$f_{i\eta F} = -K_{\eta F} (\eta_{iF} - \eta_{iF0}) - B_{\eta F} [-(y_{iF} - y_{iF0})]^{v_{\eta}} (\dot{\eta}_{iF} - \dot{\eta}_{iF0}), \quad v_x = 1.0, \quad v_y = 0.9 \quad (4)$$

where x_{iF0} and y_{iF0} are the coordinates of foot i touchdown and v_{η} is a parameter dependent on the ground characteristics. The values for the parameters $K_{\eta F}$ and $B_{\eta F}$ (Table 1) are based on the studies of soil mechanics [11].

Robot model parameters		Locomotion parameters	
S_P	1 m	L_S	1 m
L_{ij}	0.5 m	H_B	0.9 m
O_i	0 m	F_C	0.1 m
M_b	88.0 kg	Ground parameters	
M_{ij}	1 kg		
K_{xH}	10^5 Nm^{-1}	K_{xF}	$1302152.0 \text{ Nm}^{-1}$
K_{yH}	10^4 Nm^{-1}	K_{yF}	$1705199.0 \text{ Nm}^{-1}$
B_{xH}	10^3 Nsm^{-1}	B_{xF}	$2364932.0 \text{ Nsm}^{-1}$
B_{yH}	10^2 Nsm^{-1}	B_{yF}	$2706233.0 \text{ Nsm}^{-1}$

Table 1: System Parameters

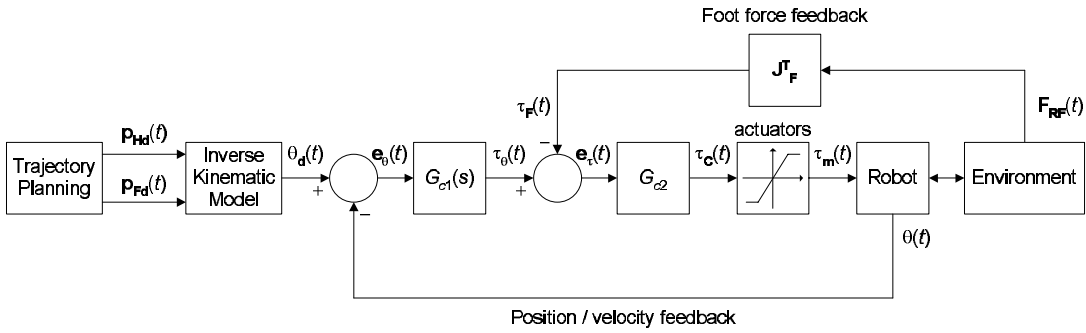


Figure 2: Quadruped robot control architecture

3.4 Control Architecture

The general control architecture of the multi-legged locomotion system is presented in Figure 2. The trajectory planning is held at the cartesian space but the control is performed in the joint space, which requires the integration of the inverse kinematic model in the forward path. The control algorithm considers an external position and velocity feedback and an internal feedback loop with information of foot-ground interaction force. On a previous work it was demonstrated the superior performance of introducing force feedback and this was highlighted for the case of having non-ideal actuators with saturation or variable ground characteristics [11].

Based on these results, in this study we adopt a PD controller for $G_{c1}(s)$ and a simple P controller for G_{c2} , with gain $Kp_j = 0.9$. For the PD algorithm we have:

$$G_{C1j}(s) = Kp_j + Kd_j s, \quad j = 1, 2 \quad (5)$$

being Kp_j and Kd_j the proportional and derivative gains.

4 Measures for Performance Evaluation

In mathematical terms we establish several global measures of the overall mechanism performance in an average sense [8, 9]. In this perspective, we define three indices $\{E_{av},$

D_{av}, T_L inspired on the system dynamics and one index $\{\varepsilon_{xyH}\}$ based on the trajectory tracking errors.

A first measure in this analysis is the mean absolute density of energy per travelled distance E_{av} . This index is computed assuming that energy regeneration is not available by actuators doing negative work, that is, by taking the absolute value of the power. At a given joint j and leg i , the mechanical power is the product of the motor torque and angular velocity. The global index E_{av} is obtained by averaging the mechanical absolute energy delivered over the travelled distance d :

$$E_{av} = \frac{1}{d} \sum_{i=1}^n \sum_{j=1}^m \int_0^T |\tau_{ijm}(t) \dot{\theta}_{ij}(t)| dt \quad [\text{Jm}^{-1}] \quad (6)$$

Although minimizing energy appears to be an important consideration, it may occur instantaneous, very high, power demands. In such cases, the average value can be small while the peaks are physically unrealisable. An alternative index is the standard deviation per meter that evaluates the dispersion around the mean absolute energy over a complete cycle T and travelled distance d :

$$P_i(t) = \sum_{i=1}^n \sum_{j=1}^m |\tau_{ijm}(t) \dot{\theta}_{ij}(t)| \quad [\text{W}] \quad (7a)$$

$$D_{av} = \frac{1}{d} \sqrt{\frac{1}{T} \int_0^T \left[P_i(t) - \frac{E_{av}}{T} d_1 \right]^2 dt}, \quad d_1 = 1 \text{ m} \quad [\text{Wm}^{-1}] \quad (7b)$$

where P_i is the total instantaneous absolute mechanical power.

A third measure consists on T_L , the density of power lost in the joint actuators per travelled distance d , that is:

$$T_L = \frac{1}{d} \sqrt{\frac{1}{T} \sum_{i=1}^n \sum_{j=1}^m \int_0^T [\tau_{ijm}(t)]^2 dt} \quad [\text{N}] \quad (8)$$

In what concerns the hip trajectory following errors we can define the index:

$$\varepsilon_{xyH} = \sum_{i=1}^n \sqrt{\frac{1}{N_s} \sum_{k=1}^{N_s} (\Delta_{ixH}^2 + \Delta_{iyH}^2)}, \quad \Delta_{i\eta H} = \eta_{iHd}(k) - \eta_{iH}(k), \quad \eta = \{x, y\} \quad [\text{m}] \quad (9)$$

where N_s is the total number of samples for averaging purposes.

In all cases the performance optimization requires the minimization of each index.

5 Simulation Results

To illustrate the use of the preceding concepts, in this section we develop a set of simulation experiments to estimate the influence of parameters β , L_S and H_B , when adopting periodic gaits.

	$V_F = 0.2 \text{ ms}^{-1}$		$V_F = 1.0 \text{ ms}^{-1}$		$V_F = 5.0 \text{ ms}^{-1}$	
$\beta = 25\%$	Kp_1	10000	Kp_1	5000	Kp_1	4000
	Kd_1	0	Kd_1	40	Kd_1	160
	Kp_2	1000	Kp_2	4000	Kp_2	500
	Kd_2	60	Kd_2	0	Kd_2	20
$\beta = 50\%$	Kp_1	5000	Kp_1	1000	Kp_1	1000
	Kd_1	80	Kd_1	200	Kd_1	100
	Kp_2	4500	Kp_2	2000	Kp_2	4500
	Kd_2	0	Kd_2	20	Kd_2	20
$\beta = 75\%$	Kp_1	3000	Kp_1	4000	Kp_1	9000
	Kd_1	180	Kd_1	200	Kd_1	80
	Kp_2	2500	Kp_2	5000	Kp_2	500
	Kd_2	0	Kd_2	20	Kd_2	40

Table 2: Quadruped Controller Parameters

In a first phase, we study a quadruped adopting the WG and then examine the variation of the performance indices with other gaits, for different controller tunings.

In a second phase, we implement several walking patterns commonly found in nature for quadrupeds. The quadruped robot is then simulated in order to compare the performance of the different gaits *versus* V_F , for different controller tunings.

In both phases the robot is controlled through a PD joint leg controller. With this algorithm, large forces occur during the feet impact with the ground, giving rise to torques that propagate through the leg mechanical structure up to the joints. In order to determine the impact influence upon the results, the experiments are repeated for an ideal case where we have the planned robot trajectories.

In all simulations, the discrete-time control algorithm is evaluated with a sampling frequency of $f_{sc} = 2.0$ kHz while the robot and environment dynamics are calculated with a sampling frequency of $f_{sr} = 20.0$ kHz.

5.1 Controller Tuning Methodology

For the system simulation we consider the robot body parameters, the locomotion parameters and the ground parameters presented in Table 1. Moreover, we assume high performance joint actuators with a maximum torque in (2) of $\tau_{ijMax} = 400$ Nm.

To tune the controller we adopt a systematic method, testing and evaluating a grid of several possible combinations of controller parameters, while establishing a compromise in what concerns the simultaneous minimization of E_{av} (6) and ε_{xyH} (9).

5.2 Locomotion Parameters versus Body Forward Velocity

In order to analyse the evolution of the locomotion parameters β , L_S and H_B with V_F , for a given gait, the robot controller is tuned for different values of the forward velocity $V_F = \{0.2 \text{ ms}^{-1}, 1.0 \text{ ms}^{-1}, 5.0 \text{ ms}^{-1}\}$ and duty factor $\beta = \{25\%, 50\%, 75\%\}$, while adopting the WG, resulting the possible controller parameters presented in Table 2.

After completing the controller tuning, the robot forward straight line locomotion is

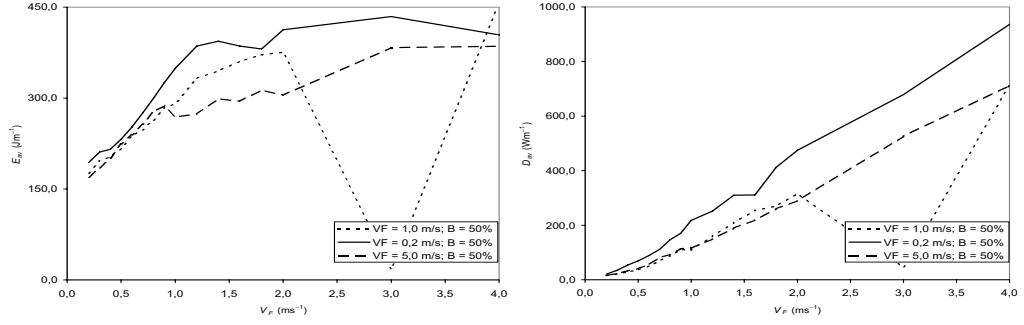


Figure 3: $\min[E_{av}(V_F)]$ (left) and $\min[D_{av}(V_F)]$ (right) for $F_C = 0.1$ m, WG

simulated for different gaits, while varying the body velocity on the range $0.2 \leq V_F \leq 4.0$ ms^{-1} . In the simulations, we consider the gaits $\{\text{Wave, Equal Phase Half Cycle, Equal Phase Full Cycle, Backward Wave, Backward Equal Phase Half Cycle, Backward Equal Phase Full Cycle}\} \equiv \{\text{WG, EPHC, EPFC, BW, BEPHC, BEPFC}\}$ [1]. For each gait and body velocity, the set of locomotion parameters (β, L_S, H_B) that minimises a given optimization index is determined.

The charts presented in Figure 3 (left) depict the minimum value of the index E_{av} , on the range of V_F under consideration, for three different robot joint leg controller tunings. It is possible to conclude that the minimum values of the index E_{av} increase with V_F , independently of the adopted controller tuning. Although not presented here, due to space limitations, the behaviour of the charts $\min[E_{av}(V_F)]$, for all other controller tunings present similar shapes.

This increase with V_F is observed on the other performance indices, irrespectively of the controller tuning adopted, as can be seen in the chart of Figure 3 (right) for the case of D_{av} .

Next we analyse how the locomotion parameters vary with V_F . Figure 4 shows that the optimal value of β decreases with V_F , while analysing the robot locomotion through the indices E_{av} and T_L , respectively. Moreover, Figure 5 (left) reveals that the optimal value of L_S must increase with V_F when considering the performance index E_{av} . Finally, Figure 5 (right) shows that H_B must decrease with V_F from the viewpoint of the performance index T_L .

The variations of the locomotion parameters (β, L_S, H_B) are similar when analysing the robot locomotion through the other performance indices and for the different robot joint leg controller tunings under consideration (Table 2).

For the other periodic walking gaits considered on this study, the evolution of the optimization indices and the locomotion parameters with V_F follows the same pattern.

Therefore, we conclude that the locomotion parameters should be adapted to the walking velocity in order to optimize the robot performance. As V_F increases, the values of β and H_B , should be decreased and the value of L_S increased.

Finally, the previous experiences are repeated for the case of the planned robot trajectories. Figure 6 shows the evolution of the locomotion parameters L_S and H_B with V_F

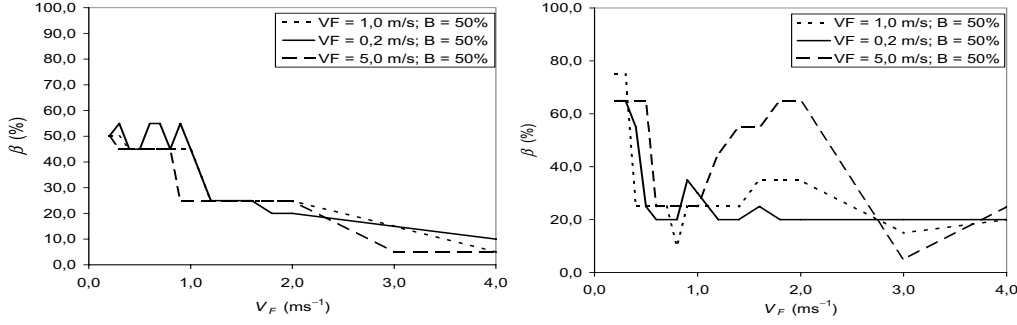


Figure 4: $\beta(V_F)$ for $\min(E_{av})$ (left) and $\beta(V_F)$ for $\min(T_L)$ (right) for $F_C = 0.1$ m, WG

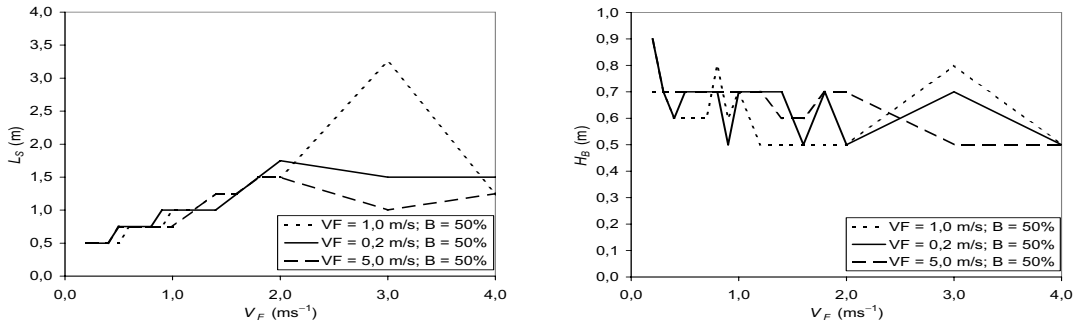


Figure 5: $L_S(V_F)$ for $\min(E_{av})$ (left) and $H_B(V_F)$ for $\min(T_L)$ (right) for $F_C = 0.1$ m, WG

when considering the performance index E_{av} . We can see that L_S must increase and H_B must decrease with V_F . These results agree with the previous ones. Regarding the optimal value of β it is independent of V_F , and must be kept small. The variations of the three locomotion parameters (β , L_S , H_B) are similar when analyzing the robot locomotion through the other performance indices. These results seem to agree with the observations of the living quadruped creatures [12].

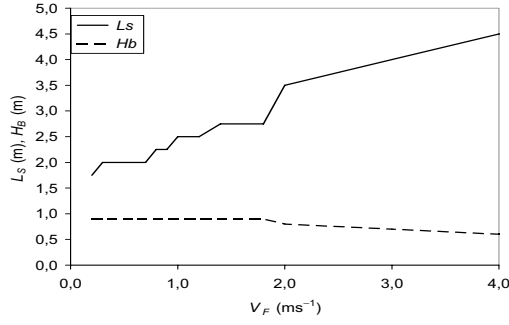
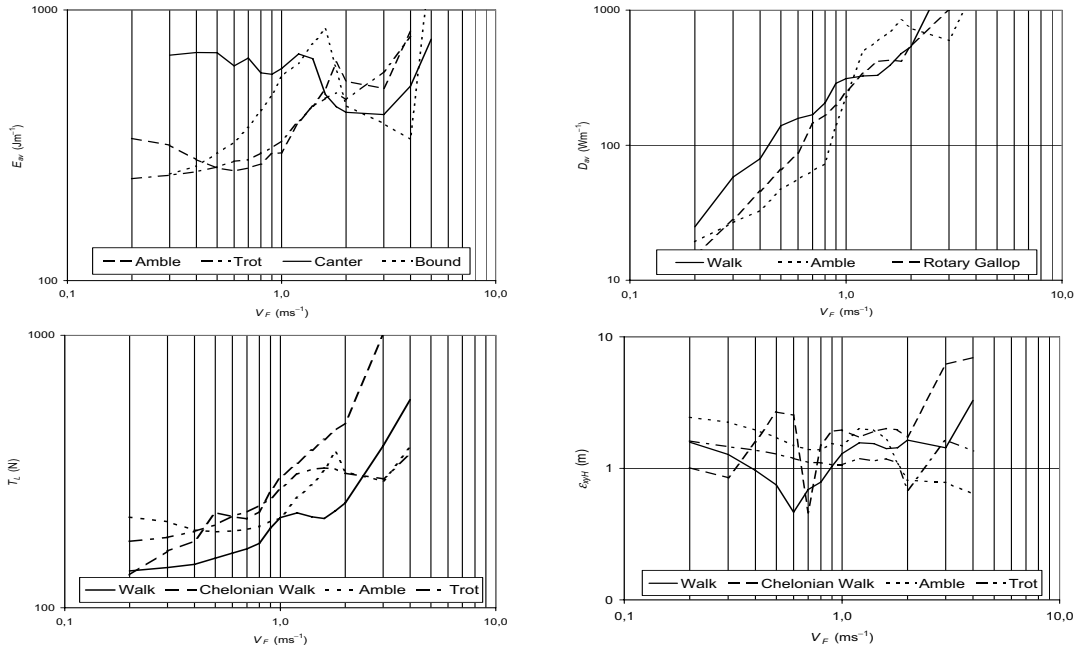
5.3 Gait Selection versus Body Forward Velocity

In a second phase we determine the best locomotion gait, at each forward robot velocity on the range $0.2 \leq V_F \leq 4.0$ ms^{-1} .

For this purpose, we test the forward straight line quadruped robot locomotion, as a function of V_F , when adopting different gaits often observed in several quadruped animals while they walk / run at variable speeds [7].

Therefore, we consider three walking gaits (Walk, Chelonian Walk and Amble), two symmetrical running gaits (Trot and Pace) and five asymmetrical running gaits (Canter, Transverse Gallop, Rotary Gallop, Half-Bound and Bound). These gaits are usually adopted by animals moving at low, moderate and high speed, respectively.

In the analysis are used the system and controller parameters (obtained for the quadruped robot walking with the WG, $V_F = 1.0$ ms^{-1} and $\beta = 50\%$) presented in Tables 1 and 2, respectively.


 Figure 6: $L_S(V_F)$ and $H_B(V_F)$ for $\min(E_{av})$ for $F_C = 0.1$ m, WG

 Figure 7: $\min[E_{av}(V_F)]$, $\min[D_{av}(V_F)]$, $\min[T_L(V_F)]$ and $\min[\varepsilon_{xyH}(V_F)]$ for $F_C = 0.1$ m

The charts of $\min[E_{av}(V_F)]$, $\min[D_{av}(V_F)]$, $\min[T_L(V_F)]$ and $\min[\varepsilon_{xyH}(V_F)]$, for the different gaits, are presented on Figure 7. The index E_{av} suggests that the locomotion should be Trot, Amble, Canter and Bound as the speed increases. The analysis through D_{av} indicates that the Rotary Gallop, Amble and Walk gaits should be adopted for low, medium and high velocities, respectively. Finally, the performance measures T_L and ε_{xyH} point out that the quadruped locomotion should adopt Chelonian Walk, Walk, Trot and Amble gaits as V_F increases. We can conclude that, from the viewpoint of each proposed optimising index, the robot gait should change with the desired forward body velocity. These results seem to agree with the observations of the living quadruped creatures [12]. However, the results from the different indices are not totally consistent with each other, with exception of T_L and ε_{xyH} (see Figure 7, lower row).

In order to analyse the influence of the controller tuning, the robot controller is re-tuned for each gait, considering a forward velocity $V_F = 1.0 \text{ ms}^{-1}$ while adopting the locomotion parameters $L_S = 1.0$ m and $H_B = 0.9$ m, leading to the controller parameters of Table 3.

Gait	Kp_1	Kd_1	Kp_2	Kd_2
Walk	1000	40	2000	40
Chelonian Walk	5000	200	2500	20
Amble	1000	20	1000	60
Trot	1000	140	2000	20
Pace	1000	60	500	40
Canter	1000	0	1500	20
Transverse Gallop	6000	40	1000	40
Rotary Gallop	4000	0	500	80
Half-Bound	4000	0	3000	20
Bound	2000	0	500	20

Table 3: Quadruped Controller Parameters

Figure 8 analyses the robot locomotion through the indices E_{av} , D_{av} , T_L and ε_{xyH} . The analysis through T_L points out that the quadruped locomotion should adopt the Chelonian Walk, Walk, Amble, Pace and, finally, the Trot gait as the robot speed increases. However, when comparing the results obtained through the other performance indices, we conclude, again, that they are not homogeneous. Analysing the results, we conclude that, from the viewpoint of each proposed optimising index, the robot gait should change with the desired forward body velocity, which seems to agree with the observations of the living quadruped creatures [12].

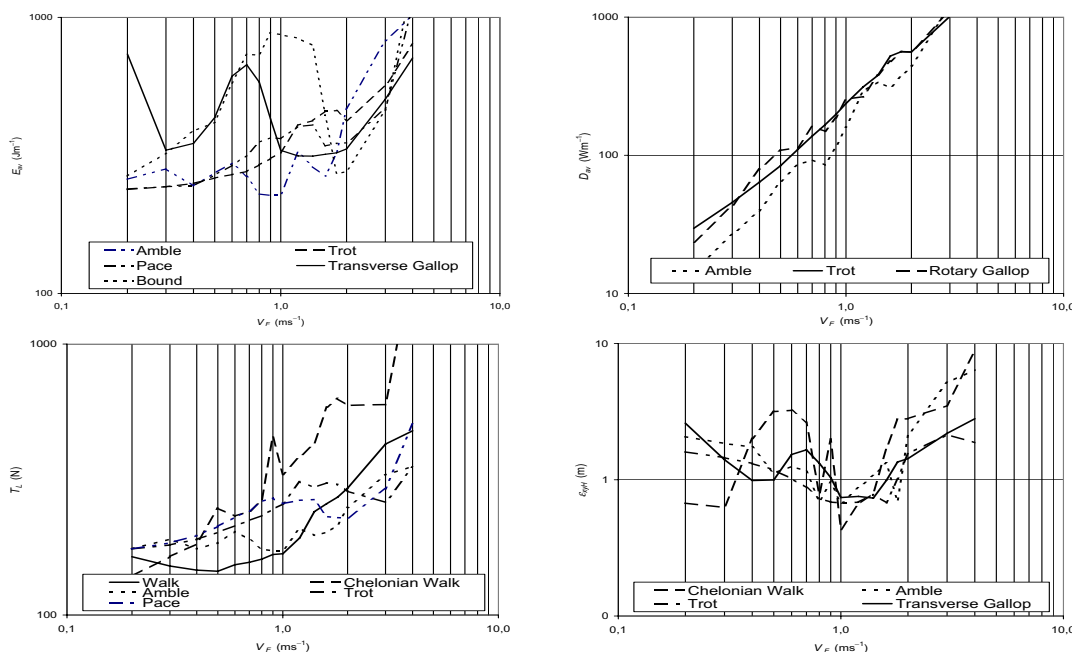


Figure 8: $\min[E_{av}(V_F)]$, $\min[D_{av}(V_F)]$, $\min[T_L(V_F)]$ and $\min[\varepsilon_{xyH}(V_F)]$ for $F_C = 0.1$ m

Finally, the previous experiences are repeated for the case of the planned robot trajectories. According to the charts presented in Figure 9, when analysing the locomotion

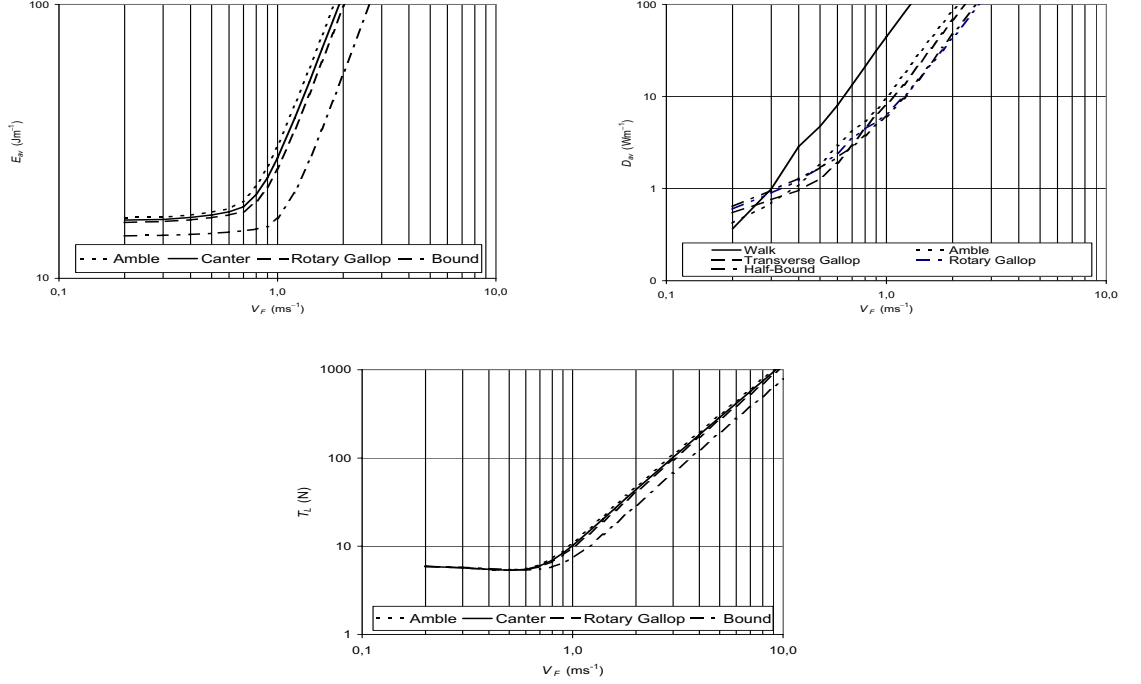


Figure 9: $\min[E_{av}(V_F)]$, $\min[D_{av}(V_F)]$ and $\min[T_L(V_F)]$ for $F_C = 0.1$ m

through the indices E_{av} and T_L the preferred gait is the Bound, on the range of V_F under study. Concerning the analysis through the index D_{av} , the quadruped should adopt the Walk, Amble, Transverse Gallop, Bound and Rotary Gallop gaits as V_F increases. Moreover, we conclude that the results obtained through the different performance indices are not homogeneous.

6 Conclusions

In this paper we have compared several dynamic aspects of multi-legged robot locomotion gaits. By implementing different motion patterns, we estimated how the robot responds to a variety of locomotion variables such as duty factor, step length and body height and to the forward speed. For analyzing the system performance four quantitative measures were defined based on the system dynamical properties and the trajectory errors. A set of experiments determined the best set of gait and locomotion variables, as a function of the robot velocity.

The results show that the locomotion parameters should be adapted to the walking velocity in order to optimize the robot performance. As the forward velocity increases, the values of β and H_B , should be decreased and the value of L_S increased. Furthermore, for the case of a quadruped robot, we concluded that the gait should be adapted to V_F .

While our focus has been on a dynamic analysis in periodic gaits, certain aspects of locomotion are not necessarily captured by the proposed measures. Consequently, future work in this area will address the refinement of our models to incorporate more unstructured terrains, namely with distinct trajectory planning concepts. The effect of distinct values of the robot intra-body compliance parameters will also be studied, since animals use their body compliance to store energy at medium and high velocities.

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